Time: 3hrs.
M.M. 100

Note: Attempt all questions.

1. Q1 to Q6 carry 1 mark each.
2. Q7 to Q19 carry 4 marks each.
3. Q20 to Q26 carry 6 marks each.

## SECTION - A

## Question number 1 to 10 carry 1 mark each.

Q1. If $P=\{4,3\}$, form the set $P \times P \times p$
Q2. Find the value of $\operatorname{Sin}\left(\frac{31 \pi}{3}\right)$
Q3. Write the following in set builder form $\{1,4,9----100\}$
Q4. If $\frac{1}{6!}+\frac{1}{7!}=\frac{x}{8!}$ find value of ' $x$ '
Q5. Solve $5 x-3<3 x+1$ when x is real.
Q6. Find the slope of line making inclination of $60^{\circ}$ with positive direction of $x$-axis.
SECTION - B

Q7. Find domain of function: $f(x)=\frac{x^{2}+3 x+5}{x^{2}-5 x+4}$.
Q8. Find the real numbers $x$ and $y$ if $(x-i y)(3+5 i)$, is the conjugate of $-6-24 i$
Q9. Find the number of different 8 - letter arrangements that can be made from the letters of word DAUGHTER so that
i) all vowels occur together.
ii) all vowels do not occur together.

Q10. A group consists of 4 girls and 7 boys. In how many ways can a team of 5 members be selected if team has
i) at least one boy and one girl
ii) at least 3 girls

Q11. Find the $(a+b)^{4}-(a-b)^{4}$, Hence evaluate $(\sqrt{3}+\sqrt{2})^{4}-(\sqrt{3}-\sqrt{2})^{4}$
Q12. Find the sum to ' $n$ ' terms of sequence $7,77,777,7777, \ldots \ldots$. .
Q13. Find the sum to ' $n$ ' terms of $n(n+1)(n+4)$
Q14. Find angles between the lines $y-\sqrt{3} x-5=0$ and $\sqrt{3} y-x+6=0$

Q15. Find distance of point $(3,-5)$ from line $3 x-4 y-26=0$
Q16. Find the equation of set of points $P$ the sum of whose distances from $A(4,0,0)$ and $B(-4,0,0)$ is equal to 10 .
Q17. Find the derivative of
(i) $\left(6 x^{3}+9 x\right)(5 x+10)$
(ii) $\frac{5 x+4}{x-3}$

Q18. Rewrite the following statement with "if - then" in four different ways conveying the same meaning.
"If a natural number is even, then its square is also even".
Q19. One card is selected from pack of 52 cards,
i) how many points are there in sample space
ii) calculate probability that card is an ace of spades
iii) calculate probability that card is king
iv) calculate probability that card is black card

## SECTION - C

Q20. In a survey of 60 people, it was found that 25 people read news paper $\mathrm{H}, 26$ read news paper T, 26 read news paper I, 9 read both H and I, 11 read both H and T, 8 read both T and I, 3 read all three newspapers. Find
(i) the number of people who read at least one of the news papers
(ii) the number of people who read exactly one newspaper

Q21.
a) Find general solution for $\operatorname{Cos} 3 x+\operatorname{Cos} x-\operatorname{Cos} 2 x=0$
b) Prove that $(\operatorname{Cos} x+\operatorname{Cos} y)^{2}+(\operatorname{Sin} x-\operatorname{Sin} y)^{2}=4 \operatorname{Cos}^{2} \frac{x+y}{2}$

Q22. Solve the following system of inequalities graphically

$$
\begin{aligned}
& x-2 y \leq 3 \\
& 3 x+4 y \geq 12 \\
& y \geq 1 \quad, x \geq 0
\end{aligned}
$$

Q23. Find co-ordinates of foci, the vertices, the length of major axis, minor axis, the eccentricity and length of latus rectum of ellipse $16 x^{2}+y^{2}=16$

Q24. Prove the following by using the Principle of Mathematical induction for all $n \in N$

$$
1.2 .3+2.3 .4+\ldots \ldots+n(n+1)(n+2)=\frac{n(n+1)(n+2)(n+3)}{4}
$$

Q25. Find mean deviation about median for the following data:

| Class | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 6 | 7 | 15 | 16 | 4 | 2 |

Q26. Solve: $x^{2}-(7-i) x+(18-i)=0$ over $C$

