# SUMMATIVE ASSESSMENT - II <br> MATHEMATICS <br> Class - X 

## Time allowed : 3 hours

Maximum Marks : 90

## SECTION-A

Question numbers 1 to 4 carry one mark each.

Does the cubes of natural numbers form an A.P. ? Give reason.
The shadow of a pole at a particular time of the day is $\frac{1}{\sqrt{3}}$ times the height of the pole. What is the elevation of the source of light?

The given spinner is spun once what is the probability of obtaining a multiple of 2 ?


Find the distance of the point $(5,-12)$ from the origin.

## SECTION-B

Question numbers 5 to $\mathbf{1 0}$ carry two marks each.
If the numbers $x-2,4 x-1$ and $5 x+2$ are in AP, then find the value of $x$.
Find the $7^{\text {th }}$ term from the end of the AP : $7,10,13, \ldots, 184$.
A triangle $A B C$ circumscribes a circle touching the sides $A B, B C, C A$ at points $P, Q, R$ respectively. If 2 $A P=6 \mathrm{~cm}, B P=8 \mathrm{~cm}$ and $A C=14 \mathrm{~cm}$, find the length of $B C$.

Draw a line segment of length 7.7 cm and divide it internally in the ratio $3: 4$.
In the figure, out of the two concentric circles, the radius of the bigger circle is 5 cm and the length of the chord $A B$ of the same circle is 8 cm , which is a tangent to the smaller circle. Find the radius of the smaller circle.


Some children, playing on the beach, dig out sand for making a hollow cylinder in the ground of radius 14 cm and depth 20 cm . They then use this sand to make a cone like structure of radius 14 cm . What is the height of the cone?

## SECTION-C

Question numbers $\mathbf{1 1}$ to 20 carry 3 marks each.
Write whether the following statements are true or false. Justify your answers.
(i) Every quadratic equation has atleast one real root.
(ii) If in a quadratic equation in $x$ the coefficient of $x$ is zero, then the quadratic equation has no real roots.

Find the sum of the first 31 terms of the AP : $9,4,-1, \ldots$
Draw an equilateral triangle of side 4 cm and then another triangle whose sides are $\frac{5}{4}$ of the corresponding sides of the first triangle.

A tower stands on a horizontal plane and is surmounted by a flagstaff of height 5 m . From a point on the plane, the angles of elevation of the bottom and the top of the flagstaff are $30^{\circ}$ and $60^{\circ}$ respectively. Find the height of the tower.

A pair of dice thrown once. What is the probability of getting a doublet of odd number ?
If $(5,2),(-3,4)$ and $(x, y)$ are collinear, show that $x+4 y-13=0$.
Find the coordinates of the centroid of a triangle whose vertices are
$\mathrm{A}(2 \sqrt{3}, \sqrt{2}), \mathrm{B}(\sqrt{27}, \sqrt{8})$ and $\mathrm{C}(\sqrt{3},-2 \sqrt{2})$.
$A B C D$ is a trapezium with $A B \| D C, A B=18 \mathrm{~cm}, D C=32 \mathrm{~cm}$ and distance between $A B$ and $D C=14 \mathrm{~cm}$. If arcs of equal radii 7 cm with centres $A, B, C$ and $D$ have been drawn, then find the area of the region of the trapezium which is not the part of the sectors drawn.

Using paper-mache, a student made a right circular hollow cone of height 15 cm and radius of base 8 cm . He then has to paint this cone from outside and inside both. Find is the total surface area that has to be painted.

A right circular cone has been placed upon cylinder. The base of the cone fully coincides with base of the cylinder and covers it. If the area of the base of the cylinder is $154 \mathrm{~cm}^{2}$, height of the cylinder is 10 cm and the volume of the entire solid is $1848 \mathrm{~cm}^{3}$, calculate the total height of the solid.

## SECTION-D

Question numbers 21 to 31 carry 4 marks each.

The sum of areas of two squares is $640 \mathrm{~m}^{2}$. If the difference of their perimeters is 64 m , find the sides of the two squares.

The sum of $n$ terms of a sequence is $3 n^{2}+4 n$. Find the $n^{\text {th }}$ term and show that the sequence is 4 A.P.

Solve : $\frac{2 y}{y-4}+\frac{2 y-5}{y-3}=\frac{25}{3} ; y \neq 3,4$.


The tangent at a point $P$ on a circle with centre $O$ meets the extended diameter BOA at $T$. If $\angle \mathrm{PBO}=30^{\circ}$, prove that $\triangle \mathrm{APT}$ is isosceles.

Construct a $\triangle \mathrm{PQR}$ in which $\mathrm{QR}=6 \mathrm{~cm}, \angle \mathrm{Q}=60^{\circ}$ and $\angle \mathrm{R}=45^{\circ}$. Construct another triangle 4 similar to $\triangle P Q R$ such that its sides are $\frac{5}{6}$ of the corresponding sides of $\triangle P Q R$.

From the top of a building, 15 m high, the angle of elevation of the top of a tower is found to be $30^{\circ}$. From the bottom of the same building, the angle of elevation of the top of the tower is found to be $60^{\circ}$. Find the height of the tower and the distance between the tower and building.

All the queens are removed from a well-shuffled deck of 52 playing cards. A card is drawn at 4 random from the remaining pack. Find the probability of drawing a.
(i) a king
(ii) a black card
(iii) a face card

If $A(3,0), B(4,5), C(-1,4)$ and $D(-2,-1)$ are four points in a plane, show that $A B C D$ is a 4 rhombus but not a square.

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A child prepares a poster on "SAVE ENERGY" on a square sheet whose each side measures 50 cm . At each corner, she draws a quadrant of a circle of radius 5 cm and at the middle, a circle of diameter 10 cm as shown in the figure. Find the area of the shaded portion. What value is depicted by the child ?
(Use $\pi=3.14$ )


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A model of a traffic signal on the road has a triangular base $A B C$ with $\angle A=90^{\circ}$ and with a red circular light within it as shown in the figure. If $A B=12 \mathrm{~cm}$ and $B C=20 \mathrm{~cm}$ and $R$ is the incentre of the $\triangle A B C$, find the area used for the red light.

The inner circumference of a circular track is 440 m . The track is 14 cm wide. Find the cost of levelling it at 20 paise/sq m . Also find the cost of putting up fencing along outer circle at ₹ 2/metre.

